Programme Code - 26

Scheme and Syllabi of Examination

for

M.Sc. Course Work

in

Mathematics

(w. e. f. academic session 2021-2022)

Offered by

Department of Basic & Applied Sciences

Under

(Faculty of Science)



Bhagat Phool Singh Mahila Vishwavidyalaya Khanpur Kalan (Sonepat), Haryana-131305



SCHEME OF STUDIES & EXAMINATIONS

M.Sc. in Mathematics (Two Year Course)

Paper No.	Paper title	Teaching Scheme			Examina	tion Schen	Duration of Exam.	Credit	
		L	Τ	Р	Internal Marks	External Marks	Total		
MAL- 501	Advanced Abstract Algebra–I	5	0	0	20	80	100	3 Hours	5
MAL- 503	Real Analysis	5	0	0	20	80	100	3 Hours	5
MAL-505	Complex Analysis-I	5	0	0	20	80	100	3 Hours	5
MA L-507	Ordinary Differential Equations-I	5	0	0	20	80	100	3 Hours	5
MAL- 509	Classical Mechanics	5	0	0	20	80	100	3 Hours	5
MAP-511	Programming in 'C' (Lab)	0	0	4	20	80	100	3 Hours	2
MAP-513	Seminar-I	0	0	2	20	•••	20	•••	1
	Total	25	0	6	140	480	620		28

Semester – I Effective from Session 2021-2022(With CBCS)



SCHEME OF STUDIES & EXAMINATIONS

M.Sc. in Mathematics (Two Year Course)

Paper No.	Paper title	Teaching Scheme		Examin	ation Sche	Duration of Exam	Credit		
		L	Т	Р	Interna Marks	External Marks	Total		
MAL- 502	Advanced Abstract Algebra-II	5	0	0	20	80	100	3 Hours	5
MAL- 504	Complex Analysis-II	5	0	0	20	80	100	3 Hours	5
MAL -506	Mathematical Statistics	5	0	0	20	80	100	3 Hours	5
MAL -508	Ordinary Differential Equations-II	5	0	0	20	80	100	3 Hours	5
MAL- 510	Methods of Applied Mathematics	5	0	0	20	80	100	3 Hours	5
MAP -512	Programming with FORTAN(Lab)	0	0	4	20	80	100	3Hours	2
MAP-514	Seminar-II	0	0	2	20		20		1
	Total	25	0	6	140	480	620		28

Semester – II Effective from Session 2021-2022(With CBCS)



SCHEME OF STUDIES & EXAMINATIONS

M.Sc. in Mathematics (Two Year Course)

Semester – III

Effective from Session 2022-2023(With CBCS)

Paper No.	Paper title	Teaching		Examination Scheme			Duration	Credit	
		Schen	Scheme					of Exam	
		L	Т	Р	Internal	External	Total		
					Marks	Marks			
MAL- 601	Measure &Integration	5	0	0	20	80	100	3 Hours	5
	Theory								
MAL- 603	Topology	5	0	0	20	80	100	3 Hours	5
MAL -605	Operations Research	5	0	0	20	80	100	3 Hours	5
	Techniques								
Open Electiv	ve(to be chosen from	4	0	0	20	80	100	3 Hours	4
the list of ele	ectives provided by the								
University)/(CBCS Paper								
	Elective-I	5	0	0	20	80	100	3 Hours	5
	Elective-II	5	0	0	20	80	100	3 Hours	5
MAP-615	MATLAB (Lab)	0	0	4	20	80	100	3Hours	2
MAP-617	Seminar-III	0	0	2	20		20		1
	Total	29	0	6	160	560	720		32

Electives:

(Students are required to take both the electives from the same Group- A)

Group-A

MAL- 607	Analytic Number Theory
MAL- 609	Mechanics of Solids-I
MAL- 611	Fluid Mechanics
MAL- 613	Advanced Discrete Mathematics

Note:Electives can be offered subject to availability of requisite resources/ faculty in the department.



SCHEME OF STUDIES & EXAMINATIONS

M.Sc. in Mathematics (Two Year Course)

Semester – IV

Effective from Session 2022-2023(With CBCS)

Paper No.	Paper title	Teaching		Examination Scheme			Duration		
		Sch	Scheme					of Exam	Credit
		L	Т	Р	Internal	External	Total		
					Marks	Marks			
MAL -602	Functional Analysis	5	0	0	20	80	100	3 Hours	5
MAL-604	Integral Equation	5	0	0	20	80	100	3 Hours	5
MAL -606	Differential Geometry	5	0	0	20	80	100	3 Hours	5
Open Elective(to be chosen from		4	0	0	20	80	100	3 Hours	4
the list of ele	ctives provided by								
the Universit	y) CBCS Paper								
	Elective-III	5	0	0	20	80	100	3 Hours	5
	Elective-IV	5	0	0	20	80	100	3 Hours	5
MAP-616	LATEX(Lab)	0	0	4	20	80	100	3Hours	2
MAP-618	Seminar-IV	0	0	2	20		20		1
	Total	29	0	6	160	560	720		32

Electives:

(Students are required to take both the electives from the group B)

Group B

MAL -608	Algebraic Coding Theory
MAL -610	Mechanics of Solids-II
MAL- 612	Advanced Fluid Mechanics
MAL- 614	Partial Differential Equations

Note:

Electives can be offered subject to availability of requisite resources/ faculty in the department.

Programme Name: M.Sc. Mathematics

Programme Outcomes

- Inculcate critical thinking to carry out scientific investigation objectively without being biased with preconceived notions
- Equip the student with skills to analyze problems, formulate an hypothesis, evaluate and validate results, and draw reasonable conclusions thereof.
- **Prepare** students for pursuing research or careers in industry in mathematical sciences and allied fields
- Imbibe effective scientific and/or technical communication in both *oral* and writing.
- Continue to acquire relevant knowledge and skills appropriate to professional activities and demonstrate highest standards of ethical issues in mathematical sciences.
- Create awareness to become an enlightened citizen with commitment to deliver one's responsibilities within the scope of bestowed rights and privileges.

Programme Specific Outcomes

- Understanding of the fundamental axioms in mathematics and capability of
- developing ideas based on them.
- Inculcate mathematical reasoning.
- Prepare and motivate students for research studies in mathematics and related fields.
- Provide knowledge of a wide range of mathematical techniques and application of mathematical methods/tools in other scientific and engineering domains.
- **Provide advanced** knowledge on topics in pure mathematics, empowering the students to pursue higher degrees at reputed academic institutions.
- Strong foundation on algebraic topology and representation theory which have strong links and application in theoretical physics, i"! Particular string theory.
- Good Understanding of number theory which can be used in modern online cryptographic technologies.
- Nurture problem solving skills, thinking, creativity through assignments, project work.
- Assist student in preparing (personal guidance, books) for competitive exams e. g. NET, Gate, etc



M.Sc. (Mathematics) 1st Semester w.e.f. 2021-2022 MAL - 501: ADVANCED ABSTRACT ALGEBRA-I

L T P 5 0 0 (5 Credits)

Marks for External Exam	: 80
Marks for Internal Exam	: 20
Total	: 100
Time	: 3 Hours

Course outcomes

- Concept of normal ,subnormal series.
- Nilpotent groups and their class of Nilpotency.
- Extension of Fields, Splitting field, Prime fields, Perfect Fields.
- Universality of Galois group, Galois Extension, Gal is Field Ability to Ability to understand Solvable groups and Derived Series
- **Note:** The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit-I

Zassenhaus's lemma, Normal, Subnormal series, Scheiers theorem, Composition Series Jordan-Holder theorem (Abelian and Non-Abelian groups), Commutators and their properties, Hall-Witt identity, three subgroup lemma of P. Hall.

Unit-II

Nilpotent groups and their class of nilpotency, Upper and lower central series and their properties, Invariant (normal) and chief series, Solvable groups and derived series.

Unit-III

Extension of Fields, Algebraic and transcendental extensions, splitting fields, normal extensions, Separable and inseparable extensions, Prime fields, perfect fields.

Unit-IV

Finite fields, Automorphisms of Extensions, fixed fields, Galois group, Galois extension, Galois fields, Fundamental theorem of Galois Theory.

References:

- 1. I.N. Herstein, Topics in Algebra, Wiley Eastern Ltd., New Delhi, 1975.
- 2. P.B. Bhattacharya, S.K. Jain and S.R. Nag Paul, Basic Abstract Algebra (2nd Edition), Cambridge University Press, Indian Edition, 1997.
- 3. M. Artin, Algebra, Prentice-Hall of India, 1991.
- 4. I.S. Luther and I.B.S. Passi, Algebra, Vol. I-Groups, Vol.II-Rings, Narosa Publishing House (Vol. I-1996, Vol. II-1999).
- 5. David S. Dummit and Richard M Foote, Abstract Algebra, Third Edition, John Wiley &Sons,Inc.USA

M.Sc. (Mathematics) 1st Semester w.e.f. 2021-2022 MAL -503: REAL ANALYSIS

L T P

5 0 0 (5 Credits)

Marks for External Exam	: 80
Marks for Internal Exam	: 20
Total	: 100
Time	: 3 Hours

Course outcomes

- Understand Riemann Stieltjes integral, its properties and rectifiable curves.
- Learn about point wise and uniform convergence of sequence and series of functions and various tests for uniform convergence.
- Find the stationary point s and extreme values of implicit functions.
- Be familar with the chain rule, partial derivatives and concept of derivation in an open subset of Rn.
- Know about Lebesgue outer measure and its properties

Note: The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit -I

Sequences and series of functions, point-wise and uniform convergence, Cauchy criterion for uniform convergence, Weierstrass M-test, Abel's and Dirichlet's tests for uniform convergence, uniform convergence and continuity, uniform convergence and Riemann-Stieltjes integration, uniform convergence and differentiation.Weierstrass approximation theorem,powerseries,uniqueness theorem for power series,Abels theorem.

Unit-II

Functions of several variables, linear transformations, derivatives in an open subset if Rn, chainrule, partial derivatives, interchange of the order of differentiation, derivatives of higher orders, Explicit and Implicit function theorem, Taylor's theorem, jacobians, extreme problems with constraints, Lagranges multiplier method.

Unit - III

Definition and existence of Riemann-Stieltjes integral, properties of the integral, integration and differentiation, the fundamental theorem of Calculus, integration of vector-valued functions, rectifiable curves.

Unit - IV

Set functions, intuitive idea of measure, elementary properties of measure, measurable sets and their fundamental properties, Lebesgue measure of sets of real numbers, algebra of measurable sets, Borel sets, equivalent formulation of measurable sets in terms of open, closed F_{σ} and G_{δ} sets, non measurable sets.

References:

- 1. W. Rudin, Principles of Mathematical Analysis (3rd edition) McGraw-Hill, Kogakusha, 1976, International Student edition.
- 2. T.M.Apostol, Mathematical Analysis, Narosa Publishing House, New Delhi, 1985.
- 3. P.K. Jain and V.P. Gupta, Lebesgue Measure and Integration, New Age International (P) Limited, New Delhi, 1986 (Reprint 2000).
- 4. H.L. Royden, Real Analysis, Macmillan Pub. Cop. Inc. 4th Edition, New York, 1993.

M.Sc. (Mathematics) 1st Semester w.e.f. 2021-2022 MAL - 505: COMPLEX ANALYSIS-I

L T P

5 0 0 (5 Credits)

Marks for External Exam: 80Marks for Internal Exam: 20Total: 100Time: 3 Hours

Course outcomes

- Analytic functions, Cauchy-Riemann differential equations, harmonic function
- Introduction of Modulus, Argument, Logarithmic and Exponentional function
- **Note:** The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit -I

Cauchy Riemann equations, Necessary and sufficient conditions for a function to be analytic,Polar form of Cauchy Riemann equations, Harmonic function ,Construction of analytical function, Power series, Radius of convergence of power series, Sum function of power series,CauchyHadamard theorem.

Unit –II

Complex Integration, Cauchy-Goursat Theorem, Simply and Multiply connected domains, Cauchy's Integral formula, Cauchy's Integral formula for higher Order derivatives, Morera's theorem, Cauchy's inequality, Liouville's theorem, The fundamental theorem of Algebra, Maximum Modulus Principle, Schwarz Lemma, Poisson's integral formula.

Unit - III

Transformation, Jacobian Transformation, Conformal Transformation ,Some general transformations, Bilinear transformations and their properties and classification.

Unit -IV

Taylor's Series, Laurent's Series, Signularities, Meromorphic functions, Argument principle, Rouche's theorem, Calculus of residues, Cauchy's residue theorem, MittagLeffler's expansion theorem.

References:

- 1. H.A. Priestly, Introduction to Complex Analysis, Clarendon Press, Oxford, 1990.
- 2. J.B. Conway, Functions of one Complex variable, Springer-Verlag, International Student-Edition, Narosa Publishing House, 1980.
- 3. L.V. Ahlfors, Complex Analysis, McGraw-Hill, 1979.
- 4. Mark J. Ablowitz and A.S. Fokas, Complex Variables: Introduction and Applications, Cambridge University Press, South Aisian Edition, 1998.
- 5. S. Ponnusamy, Foundations of Complex Analysis, Narosa Publishing House, 1997.
- 6. J.W. Brown and R.V. Churchill, Complex Variables and Applications, MC Graw Hill.

M.Sc. (Mathematics) 1st Semester w.e.f. 2021-2022 MAL- 507: ORDINARY DIFFERENTIAL EQUATIONS-I

L T P

5 0 0 (5 Credits)

Marks for External Exam	: 80
Marks for Internal Exam	: 20
Total	: 100
Time	: 3 Hours

Course outcomes

- Ordinary Differential Equation and linear system of ODE.
- Cauchy Peano Existence and uniqueness theorem.
- Picard-Lindelof theorem, Continuation of solution.
- Properties of Harmonic and Sub harmonic functions.
- Solution of dirichlet problem.
- **Note:** The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit-I

Initial-value problem and the equivalent integral equation, ε -approximate solution, Cauchy-Euler construction of an ε -approximate solution, Equicontinuous family of functions, Ascoli-Arzela theorem, Cauchy-Peano existence theorem.

Uniqueness of solutions, Lipschitz condition, Picard-Lindelof theorem for local existence and uniqueness of solutions, solution of initial-value problems by Picard method,

Unit-II

Total differential Equations: Condition of Integrability, Methods of Solution, Gronwall's differential inequality, comparison theorems involving differential inequalities, zeros of solutions, Riccati's Equation, Pruffer transformation, Lagrange's identity and Green's Formula for second-order equation

Unit-III

Sturms separation and comparison theorems. Sturm-Liouville boundary-value problems, properties of eigen values and eigen functions. Separation variable method for heat and wave equation (one dimensional) and Laplace equation in (two dimensional) in Cartesian system.

Unit-IV

Introduction solution of linear differential equation of second order, complete solution in terms of known integral, Removal of the first derivative, transformation of the equation by changing the independent variable, method of variation of parameters and method of operational factors.

References:

- 1. E.A. Coddington and N. Levinson, Theory of Ordinary Differential Equations, McGraw Hill, NY, 1955.
- 2. G. Birkhoff and G.C. Rota, Ordinary Differential Equations, John Wiley and Sons Inc..NY, 1978.
- 3. S.L. Ross, Differential Equations, John Wiley and Sons Inc., NY, 1984.
- 4. W.E. Boyce and R.C. Diprima, Elementary Differential Equations and Boundary Value Problems, John Wiley and sons Inc., NY, 1986.
- 5. Philip Hartman, Ordinary Differential Equations, John Wiley & Sons, NY 1964.

M.Sc. (Mathematics) 1st Semester w.e.f. 2021-2022 MAL -509:CLASSICAL MECHANICS

L T P

5 00 (5 Credits)

Course outcomes

- Marks for External Exam: 80Marks for Internal Exam: 20Total: 100Time: 3 Hours
- Be familiar with the concept of momental ellipsoid, equimomental system and general motion of a rigid body.
- Understand ideal constraints, general equation of dynamics and Langrange's equation for potential forces .
- Describe Hamiltonian function ,Poincare carton integral invariants and principle of least action.
- **Note:** The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit-I

Moments and products of Inertia, Theorems of parallel and perpendicular axes, principal axes, The momental ellipsoid, Equimomental systems, Coplanar distributions, Generalized coordinates, Holonomic and Non-holonomic systems, Scleronomic and Rheonomic systems, Lagrange's equations for a holonomic system.

Unit-II

Lagrange's equations for a conservative and impulsive forces, Kinetic energy as quadratic function of velocities, Generalized potential, Energy equation for conservative fields.

Hamilton's variables, Donkin's theorem, Hamilton canonical equations, Cyclic coordinates, Routh's equations, Poisson's Bracket, Poisson's Identity, Jacobi-Poisson Theorem.

Unit -III

Hamilton's Principle, Principle of least action, Poincare Cartan Integral invariant, Whittaker's equations. Jacobi's equations, Hamilton-Jacobi equation, Jacobi's theorem, Method of separation of variables, Lagrange Brackets, Condition of canonical character of a transformation in terms of Lagrange brackets and Poisson brackets, Invariance of Lagrange brackets and Poisson brackets under canonical transformations.

Unit -IV

Gravitation: Attraction and potential of rod, disc, spherical shells and sphere, Laplace and Poisson equations, Work done by self-attracting systems, Distributions for a given potential, Equipotential surfaces, Surface and solid harmonics, Surface density in terms of surface harmonics.

References:

- 1. F. Chorlton, A Text Book of Dynamics, CBS Publishers & Dist., New Delhi.
- 2. F.Gantmacher, Lectures in Analytic Mechanics, MIR Publishers, Moscow, 1975.
- 3. Louis N. Hand and Janet D. Finch, Analytical Mechanics, Cambridge University Press, 1999

M.Sc. (Mathematics) 1st Semester w.e.f. 2021-2022 MAP- 511: PROGRAMMING IN 'C'

L	Т Р	Marks for External Exam	: 80
0	04(02 Credits)	Marks for Internal Exam	: 20
		Total	: 100
		Time	: 3 Hours

Course outcomes

- Write and run a C Program along with gradual improvement using efficient error handling.
- Implement selective structures and repetitive structure in C programs using different control statements.
- To emphasize on the importance of use of pointers for efficient C programming .
- Use structure and union in a C program for handling multivariate data. List of Programs using C :
- 1. Program to generate prime numbers upto a given number.
- 2. Program to find factorial using recursion.
- 3. Program to find fibonacci terms without recursion.
- 4. Program to generate table of a number.
- 5. Program to find roots of a quadratic equation.
- 6. Program to generate fibonacci series with recursion.
- 7. Program to find factorial without recursion.
- 8. Program to find $S = \sum_{n=1}^{10} 1/(n-7)$, n!=7.
- 9. Program to find element from a given array.
- 10. Program to find transpose of a matrix.
- 11. Program to swap two numbers using pointers.
- 12. Program to arrange a string in alphabetical order.
- 13. Program to convert decimal number into octal and hexadecimal.
- 14. Program to find matrix multiplication.
- 15. Program to find arithmetic mean, variance, S.D.
- 16. Program to check whether a number is prime or not.
- 17. Program to print sum of digits.
- 18. Program to reverse a given number.

MAP- 513: SEMINAR

L T P 2 0 0 (2 Credits)

Marks for Internal Exam : 20 : 20 Total

M.Sc. (Mathematics) 2nd Semester w.e.f. 2021-2022 MAL - 502: ADVANCED ABSTRACT ALGEBRA-II

L T P

5 0 0 (5 Credits)

Marks for External Exam: 80Marks for Internal Exam: 20Total: 100Time: 3 Hours

Course outcomes

- Concept of Modules and Submodules.
- Noetherian and Artinian modules.
- Canonical Forms: Nilpotent transformation, Index of Nilpotency.
- Know about Weddernburn-Artin Theorem.
- Jordan Blocks, Jordan Form, The Primary Decomposition Theorem .
- Ability to understand/obtain the roots of a polynomial equation if the same has (or can be reduced to) degree less than five.
- Facility in working with finite fields
- Applying the concept of a field extension to various mathematical problems induding geometric constructions and perfect division of a circle into n parts
- **Note:** The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit -1

Opposite rings, Modules and submodules, Cyclic modules, Simple Modules, Schur's Lemma. Free modules, fundamental structure theorem for finitely generated abelian groups and its application to finitely generated abelian groups.

Unit-2

Noetherian and Artinian modules and rings , Hilbert basis theorem, Homomorphism (R,R,), Wedderburn-Artin theorem.

Unit -3

Canonical Forms: Similarity of linear transformations, Invariant subspaces, Reduction to triangular forms, Nilpotent transformations, Index of nilpotency, Cyclic subspace with respect to nilpotent transformation. Invariants of a nilpotent transformation.

Unit-4

The primary decomposition theorem, Jordan blocks and Jordan forms, rational canonical form, generalized Jordan form over any field. Elementary divisors of a transformation.

References:

- 1. I.N. Herstein, Topics in Algebra, Wiley Eastern Ltd., New Delhi, 1975.
- 2. P.B. Bhattacharya, S.K. Jain and S.R. Nag Paul, Basic Abstract Algebra (2nd Edition), Cambridge University Press, Indian Edition, 1997.
- 3. P.M. Cohn, Algebra, Vols. I, II & III, John Wiley & Sons, 1982, 1989, 1991.
- 4. N. Jacobson, Basic Algebra, Vols. I & II, W.H. Freeman, 1980.
- 5. I.S. Luther and I.B.S. Passi, Algebra, Vol. I-Groups, Vol.II-Rings, Narosa Publishing House, Vol. I-1996, Vol. II-1999.

M.Sc. (Mathematics) 2nd Semester w.e.f. 2021-2022 MAL – 504: Complex Analysis-II

L T P 5 0 0 (5 Credits)	Marks for External Exam Marks for Internal Exam Total	: 80 : 20 : 100
	Time	: 3 Hours

Course outcomes

- Understand the concepts of Gamma function and its properties.
- Get familiar with Riemann Zeta function, Riemann functional equation and Mittag Leffler theorem.
- Demonstrate the idea of Harnack Inequality, Dirichlet region, Green function and its properties.
- Understand the concept of integral functions, their factorisation, order and exponent of convergence
- **Note:** The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit -1

Spaces of Analytic functions, Hurwitz's theorem, Montel's theorem, Riemann mapping theorem, Weierstrass factorization theorem, Gamma function and its properties, Riemann Zeta function, Riemann's functional equation. Runge's theorem.

Unit -I1

Analytic Continuation, Uniqueness of direct analytic continuation, Uniqueness of analytic continuation along a curve, power series method of analytic continuation. Monodromy theorem and its consequences, Harmonic function on a disk, Harnack's inequality and theorem, Dirichlet problem.Green's functions.

Unit -III

Canoncial products, Jensen's formula.Poisson-jensen formula.Hadamard's three circles theorem.Order of an entire function.Exponent of Convergence.Borel's theorem.Hadamard's factorization theorem.

Unit- IV

The range of an analytic function.Bloch's theorem.The little Picard theorem.Schottky's theorem.Montel Caratheodory and the Great Picard theorem. Univalent functions. Bieberbach's conjecture (Statement only) and the "¼ theorem" (Statement only).

References:

- 1. H.A. Priestly, Introduction to Complex Analysis, Clarendon Press Oxford, 1990.
- 2. J.B. Conway, Functions of one Complex variable, Springer-Verlag, International Student-Edition, Narosa Publishing House, 1980.
- 3. L.V. Ahlfors, Complex Analysis, McGraw-Hill, 1979.
- 4. Mark J. Ablowitz and A.S. Fokas, Complex Variables: Introduction and Applications, Cambridge University Press, South Asian Edition, 1998.
- 5. S. Ponnusamy, Foundations of Complex Analysis, Narosa Publishing House, 1997.
- 6. J.W. Brown and R.V. Churchill, Complex variable and Applications, McGraw Hill.

M.Sc. (Mathematics) 2nd Semester w.e.f. 2021-2022 MAL - 506: MATHEMATICAL STATISTICS

L T P

5 0 0 (5 Credits)

Marks for External Exam	: 80
Marks for Internal Exam	: 20
Total	: 100
Time	: 3 Hours

Course outcomes

- Understand the mathematical basis of probability and its applications in various fields of life.
- Use and apply the concepts of probability mass/density functions for the problems involving single/bivariate random variables.
- Have competence in practically applying the discrete and continuous probability distributions along with their properties.
- Decide as to which test of significance is to be applied for any given large sample problem.
- **Note:** The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit -I

Sample spaces, random variables, Distribution and density distribution function, Marginal and conditional distribution, Mathematics expectation, Moments, moment generating function, cumulants, cumulants generating function, characteristic function,

Unit-II

Probability distributions: Binomial, Poisson, Geometric, Uniform and Exponential, distributions.(Detailed Theory)

Unit -III

Normal distribution, Gamma distribution, t, f, and Chi-square distribution as sampling distributions, Weak law of large numbers, Central limit theorem.

Unit -IV

Correlation: Karl Pearson coefficient of correlation, Rank correlation, Partial and multiple correlation and their Cofficients, Yules notations.

Regression: lines of regression, regression curves, regression coefficients and its properties, angle between two lines of regression, Plane of regression

References:

- 1. R.V.Hogg&A.T.Craig:Introduction to Mathematical Statistics,AmerindPub.Co.Pvt.Ltd.New Delhi,1972
- 2. S.C. Gupta and V.K Kapoor, Fundamentals of Mathematical Statistics, S. Chand & Sons, Educational Pub., New Delhi
- 3. Schaum series outlines, Mathematical Statistics.

M.Sc. (Mathematics) 2nd Semester w.e.f. 2021-2022 MAL - 508: ORDINARY DIFFERENTIAL EQUATIONS-II

L	Т	Р	Marks for External Exam	: 80
5	0	0(5 Credits)	Marks for Internal Exam	: 20
			Total	: 100
			Time	: 3 Hours

Course outcomes

- Learn about linear system, fundamental set and fundamental matrix of a homogenous system and non-homogenous system.
- Classification of critical points-rotation points, nodes, foci, saddle points.
- Liapunov function .
- Learn methods to solve various mathematical and physical problems using variational techniques.
- **Note:** The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit -I

Linear systems, fundamental set and fundamental matrix of a homogeneous system, Wronskian of a system. Method of variation of constants for a non-homogeneous system, reduction of the order of a homogeneous system, systems with constant coefficients, adjoint systems, periodic solutions, Floquet theory for periodic systems (Relevant topics from the book by Coddington and Levinson).

Unit -II

Nonlinear differential equations, plane autonomous systems and their critical points, classification of critical points-rotation points, foci, nodes, saddle points. Stability, asymptotical stability and unstability of critical points, almost linear systems, Perturbations, Simple Critical points, dependence on a parameter.

Unit -III

Liapunovfunction, Liapunov's method to determine stability for nonlinear systems, limit cycles, Bendixson non-existence theorem, Statement of Poincare-Bendixson theorem, index of a critical point (Relevant topics from the books of Birkhoff& Rota, and by Ross).

Unit -IV

Motivating problems of calculus of variations, shortest distance, minimum surface of revolution, Brachistocrone problem, isoperimetric problem, geodesics, Fundamental lemma of calculus of variations, Eulers equation for one dependent function and generalization to n dependent functions and to higher order derivatives, conditional extremum under geometric constraints and under integral constraints. (Relavant topics from the book Gelfand and Fomin)

References

- 1. E.A.Coodington and N. Levinson. Theory of Ordinary Differential Equations, McGraw Hill, NY, 1955.
- 2. G.Birkhoffand G.C.Rota, Ordinary Differential Equations, John Wiley and Sons , NY, 1978.
- 3. S.L. Ross. Differential Equations, John Wiley and Sons inc., NY, 1984.
- 4. J M Gelfand and Fomin ,S V ,Calculation of variations, Prentice hall, new Delhi, 1963.
- 5. W.E. Boyce and R.C. Diprima, Elementary Differential Equations and Boundary Value Problems, John Wiley and Sons Inc., NY, 1986.
- 6. Philip Hartman, Ordinary Differential Equations, John Wiley & Sons, NY, 1964.

M.Sc. (Mathematics) 2nd Semester w.e.f. 2021-2022 MAL -510: METHODS OF APPLIED MATHEMATICS

L T P

5 0 0 (5 Credits)

Marks for External Exam	: 80
Marks for Internal Exam	: 20
Total	: 100
Time	: 3 Hours

Course outcomes

- Understand the concept of Fourier series, Fourier integral and Fourier transform.
- Analyze the properties of Hankel transform and Mellin transform.
- Area, volume and surface areas in Cylindrical and spherical co-ordinates.
- Definition of Asymptotic sequence, expansions and series
- **Note:** The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit -I

Fourier Transforms: Definition and properties, Fourier transform of some elementary functions, convolution theorem, Application of Fourier transforms to solve ordinary & partial differential equations.

Unit -II

Curvilinear Co-ordinates: Co-ordinate transformation, Orthogonal Co-ordinates, Grad, Div, Curl, Laplacian in Orthogonal Co-ordinates, Cylindrical and Spherical Co-ordinates, expressions for velocity and accelerations, ds, dv and ds² in orthogonal co-ordinates, Areas, Volumes and

Surface areas in Cartesian, Cylindrical & Spherical co-ordinates, Contravariant and Co-variant components of a vector, Metric coefficients & Volume elements.

Unit -III

MellinTransforms:Elementary properties, Mellin Transforms of derivatives and integrals,Inversion and Convolution theorem,solution of some integral equation.Hankel Transforms: Elementary properties,Inversion theorem, Hankel Transforms of derivatives and some elementary function,relation between Fourier and Hankel transform.Asymptotic methods-Introduction.Asymptotic analysis of sums.

Unit-IV

Asymptotic approximation: Order notation, Defination of Asymptotic sequence, Expansions and series, Integration by parts and Watson Lemma, Laplace Method of Steepest decent with examples.

References:

- 1. I.N Sneddon., The Use of Integral Transforms, McGraw Hill, 1972.
- 2. Murray and R.Spiegel, Vector Analysis, Schaum's Series.

M.Sc. (Mathematics) 2nd Semester w.e.f. 2021-2022 MAL-512: PROGRAMMING WITH FORTRAN (Lab)

L T P

0 04(02 Credits)

Marks for External Exam: 80Marks for Internal Exam: 20Total: 100Time: 3 Hours

Course outcomes

- Write and run a program along with gradual improvement using Efficient error handling.
- Implement selective structures and repetitive structure s in programs using different control statements.
- Using FORTRAN find solution of ODE and simultaneous linear alegrabic equations.
- Program to find transpose of a matrix and matrix multiplication

List of programs using Fortran:

- 1. Numerical Integration
- 2. Numerical solutions of equations (single variable)
- 3. Numerical solution of simultaneous linear algebraic equations
- 4. Numerical solution of ordinary differential equation
- 5. Numerical Solution of second order ordinary differential equations.
- 6. Generate prime numbers upto a given number.
- 7. Factorial using recursion.
- 8. Find fibonacci terms without recursion.
- 9. Generate table of a number.

- 10. Find roots of a quadratic equation.
- 11. Generate fibonacci series with recursion.
- 12. Find factorial without recursion.
- 13. Find $S = \sum_{n=1}^{10} 1/(n-7)$, n!=7.
- 14. Find element from a given array.
- 15. Find transpose of a matrix.
- 16. Find matrix multiplication.
- 17. Fnd arithmetic mean, variance, S.D.
- 18. Check whether a number is prime or not.

MAP- 514: SEMINAR

- L T P
- 2 0 0 (2 Credits)

Marks for Internal Exam	: 20
Total	: 20

M.Sc. (Mathematics) 3rd Semester w.e.f. 2022-2023 MAL -601: MEASURE AND INTEGRATION THEORY

L T P

5 0 0 (5 Credits)

Marks for External Exam	: 80
Marks for Internal Exam	: 20
Total	: 100
Time	: 3 Hours

Course outcomes

- Describe the shortcomings of Riemann integral and benefits of Lebesgue integral.
- Understand the fundamental concept of measure and Lebesgue measure .
- Learn about the differentiation of monotonic function and use of fundamental theorem of calculus.
- **Note:** The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit – I

Measurable functions and their equivalent formulations, Properties of measurable functions. Approximation of measurable functions by sequences of simple functions, Measurable functions as nearly continuous functions, Egoroffs theorem, Lusin's theorem, Convergence in measure and F. Riesz theorem for convergence in measure, Almost uniform convergence.

Unit – II

Shortcomings of Riemann Integral.Lebesgue Integral of a bounded function over a set of finite measure and its properties, Lebesgue integral as a generalization of Riemann integral, Bounded convergence theorem, Lebesgue theorem regarding points of discontinuities of Riemann integrable functions,

Unit – III

Integral of non-negative functions, Fatou's Lemma, Monotone convergence theorem, General Lebesgue Integral, Lebesgue convergences theorem. Vitali's covering Lemma, Differentiation of monotonic functions,

Unit – IV

Functions of bounded variation and its representation as difference of monotonic functions,Differentiation of indefinite integral.Fundamental Theorem of Calculus.Absolutely continuous functions and their properties.

References:

- 1. Walter Rudin, Principles of Mathematical Analysis (3rd edition) McGraw-Hill, Kogakusha, 1976, International Student edition.
- 2. T.M.Apostol, Mathematical Analysis, Narosa Publishing House, New Delhi, 1985.
- 3. P.K. Jain and V.P. Gupta, Lebesgue Measure and Integration, New Age International (P) Limited Published, New Delhi, 1986 (Reprint 2000)
- 4. H.L. Royden, Real Analysis, Macmillan Pub. Co. Inc. 4th Edition, New York, 1993.
- 5. Walter Rudin, Real and Complex Analysis, Tata McGraw Hill Publishing Co. Ltd., New Delhi, 1966.

M.Sc. (Mathematics) 3rd Semester w.e.f. 2022-2023 MAL - 603: TOPOLOGY

L T P 5 0 0(5 Credits)

Marks for External Exam	: 80
Marks for Internal Exam	: 20
Total	: 100
Time	: 3 Hours

Course outcomes

- Get familiar with the concepts of topological space and continuous functions.
- Generate new topologies from a given set with bases.
- Describe the concept of homeomorphism and topological invariants.
- Establish connectedness and compactness of topological spaces and proofs of related theorems.
- Have in-depth knowledge of separation axioms and their properties
- **Note:** The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit-I

Definition and examples of topological spaces, Neighborhoods, Interior point and interior of a set, Closed set as a complement of an open set, Adherent point and limit point of a set, Closure of a set, Derived set, Properties of Closure operator, Boundary of a set, Dense subsets, Interior, Exterior and boundary operators.

Base for a topology, Neighbourhood system of a point and itsproperties, Base for Neighbourhood system Relative(Induced) topology, Alternative methods of defining a topology in terms of neighbourhood system and Kuratowski closure operator, Intersection and union of topologies on a set.

Unit-II

Continuous functions, Open and closed functions, Homeomorphism ,Connectedness and its characterization, Connected subsets and their properties, Continuity and connectedness, Connectedness spaces, Components, Locally connected spaces.

Unit- III

First and Second Countable spaces and , Lindelof's theorem, Separable spaces, Separation axioms, T_0 , T_1 and T_2 spaces their characterization and basic properties, Regular and normal spaces, Urysohn's Lemma and Tietze Extension theorem, T_3 and T_4 spaces, Complete regularity and Complete normality. $T_{3\frac{1}{2}}$ and T_5 spaces.

Unit - IV

Compact spaces and subsets, Compactness in terms of finite intersection property, Continuity and compact sets, Basic properties of compactness, Closedness of compact subset and a continuous map from a compact space into a Hausdorff space and its consequence. Sequentially and countably compact sets, Local compactness.

References:

- 1. W.J. Pervin, Foundations of General Topology, Academic Press Inc. New York, 1964.
- 2. J.L. Kelley, General Topology, Van Nostrand, Reinholkd Co., New York, 1995.
- 3. James R Munkres, Topology, A First Course, Prentice Hall of India Pvt. Ltd., New Delhi, 2000.
- 4. George F. Simmons, Introduction to Topology and Modem Analysis, McGraw-Hill,
- 5. J. Dugundji, Topology, Allyn and Bacon, 1966 (Reprinted in India by Prentice Hall Of India Pvt. Lt.).

M.Sc. (Mathematics) 3rd Semester w.e.f. 2022-2023 MAL -605: OPERATIONS RESEARCH TECHNIQUES

LTP

5 0 0 (5 Credits)

Marks of External Exam: 80Marks of Internal Exam: 20Total Marks:100Time:3 Hours

Course outcomes

- Identify and develop operations research model describing a real life problem.
- Understand the mathematical tools that are needed to solve various optimization problems.
- Solve various linear programming, transportation, assignment, queuing, inventory and game problems related toreal life.

Note: The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and

will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit – I

Operations Research : Origin, Defination and scope.

Linear programming : Formulation and solution of linear programming problems by graphical and simplex methods, Big-M and two-phase methods, Degeneracy, duality in linear programming.

Unit – II

Transportation Problems: Basic feasible solutions, Optimum solution by stepping stone and modified distribution methods, Unbalanced and degenerate problems, Transhipmentproblem. Assignment problems : Hungarian method, Unbalanced problem, Case of maximization, Travelling sellsman and crewassignments problems.

$\mathbf{Unit}-\mathbf{III}$

Concepts of stochastic processes, Poisson process, Birth-death process, Queuing models: Basic components of queuing system, Steady-state solution of Markovian queuing models with single and multiple servers (M/M/1. M/M/C, M/M/1/K, M/MC/K).

Unit-IV

Inventary control models: Economic order quantity(EOQ) model with uniform demand, EOQ when shortages are allowed, EOQ with uniform replenishment, Inventory control with price breaks.

Game theory : Two person zero sum game, Game with saddle points, The role of dominance; Algebric, Graphical and linear programming methods for solving mixed strategy games.

References:

- 1. H.A. Taha, Operation Research- An introduction, Printice Hall of India.
- 2. P.K. Gupta and D.S. Hira. Operations Research, S. Chand and Co.
- 3. S.D. Sharma, Operation Research, KedarNath Ram Nath Publications.
- 4. J.K. Sharma, Mathematical model in Operation Research, Tata McGraw Hill.

M.Sc. (Mathematics) 3rd Semester w.e.f. 2022-2023 MAL -607: ANALYTIC NUMBER THEORY (elective)

L	Т	Р

5 0 0 (5 Credits)

Marks of External Exam: 80 Marks of Internal Exam: 20 Total Marks :100 Time :3 Hours

Course outcomes

- Know about the classical results related to prime numbers and get familiar with the irrationality of e and n.
- Learn about the Fermat no. and their applicability
- Learn about arithmetic functions and about perfect numbers .Understand the representation of numbers by two or four squares

Note: The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and

will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

UNIT-I

Primes in certain arithmetical progressions.Fermat numbers and Mersenne numbers.Approximation of irrational numbers by rationals. Hurwitz's theorem, irrationality of e and π . System of linear congruences Chinese Remainder Theorem.Quadratic residues and non-residues.Legendre's Symbol.Gauss Lemma and its applications. Quadratic Law of Reciprocity jacobi's Symbol.

UNIT-II

Riemann Zeta Function $\xi(s)$ and its convergence. Application in prime numbers. $\xi(s)$ as Euler's product. Evaluation of $\xi(2)$ and $\xi(2k)$. Dirichlet series with simple properties. Dirichlet series as analytic function and its derivative. Eulers products. Introduction to modular forms.

UNIT-III

Euler's summation formula and some elementary asymptotic formula. Average order of the arithmetical functions d(n), $\sigma_{\alpha}a(n)$, $\phi(n)$, $\mu(n)$ and $\Lambda(n)$. Partial sums of a Dirichlet product and their application to $\mu(n)$ and $\Lambda(n)$.

UNIT-IV

Chebyshev's functions $\Psi(x)$ and v(x) and relation between v(x) and $\pi(x)$. Shapiro's Tauberian theorem and its applications. Partial sums of the Mobius function. Selberg's asymptotic formula.

Refrences:

- 1. T.M. Apostol. Introduction to Analytic number theory (Narosa Publishing House 1980).
- 2. T.M. Apostol. Modular functions and Dirichlet series in Number Theory (Springer-Verlag 1976).
- 3. J.P. Serre. A Course in Arithmetic G.T.M. Vol.7 (Springer Verlag 1973).

M.Sc. (Mathematics) 3rd Semester w.e.f. 2022-2023 MAL609: MECHANICS OF SOLIDS-I (elective)

- L T P
- 5 0 0 (5 Credits)

Marks of External Exam: 80Marks for Internal Exam: 20Total: 100Time: 3 Hours

Course outcomes

- Get familiar with Cartesian tensors, as generalization of vectors and their properties which are used in the analysis of stress and strain to describe the phenomenon of solid mechanics.
- Analyse the basic properties of stress and strain components, their transformations, extreme values, invariants and Saint-Venant principle of elasticity.
- Demonstrate generalized Hooke's law for three dimensional elastic solid which provides the linear relationship between stress components and strain components.

- Use different types of elastic symmetries to derive the stress-strain relationship for isotropic elastic materials for applications to architecture and engineering
- **Note:** The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit -1

Cartesian Tensor : Coordinate transformation, Cartesian Tensor of different order, Sum or difference and product of two tensors. Contraction theorem, Quotient law, Symmetric &Skew-symmetric tensors, Kronecker tensor, alternate tensor and relation between them, Scalar invariant of second order tensor, Eigen values & vectors of a symmetric second order tensor, Gradient, divergence & curl of a tensor field.

Unit -I1

Analysis of Strain : Affine transformations. Infinitesimal affine deformation.Geometrical interpretation of the components of strain.Strain quadric of Cauchy. Principal strains and invariants. General infinitesimal deformation. Saint- Venant's equations of Compatibility

Unit-III

Analysis of Stress: Stress tensor. Equations of equilibrium.Transformation of coordinates.Stress quadric of Cauchy.Principal stress and invariants.Maximum normal and shear stresses.

Unit- IV

Equations of Elasticity: Generalised Hooke's law. Homogeneous isotropic media.Elastic moduli for isotropic media.Equilibrium and dynamic equations for an isotropic elastic solid. Strain energy function and its connection with Hooke's law. BeItrami-MicheII compatibility equations. Saint- Venant's principle.

Reference:

- 1. I.S. Sokolnikoff, Mathematical Theory of Elasticity, Tata McGraw Hill Publishing Company Ltd., New Delhi, 1977.
- 2. Shanti Narayan, Text Book of Cartesian Tensors, S. Chand & Co., 1950.
- 3. S. Timoshenko and N. Goodier, Theory of Elasticity, McGraw Hill, New York, 1970.

M.Sc. (Mathematics) 3rd Semester w.e.f. 2022-2023

MAL- 611: FLUID MECHANICS (elective)

L T P

5 0 0 (5 Credits)

Marks of External Exam: 80Marks for Internal Exam: 20Total: 100Time: 3 Hours

Course outcomes

• Irrotational motion in two dimensions.Description of fluid, stream line, path line and streak lines and stream tube.

- Classification of flows- steady, unsteady, uniform non-uniform, laminar, turbulent, rotational, irrotational flows, Equation of continuity for one, two, three dimens.
- Laws of fluid friction Darcy's equation, minor losses Pipes in series- pipes in parallel- total energy line and hydraulic gradient line
- **Note:** The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit-I

Kinematics of fluid-Lagrangian and Eulerian methods, Stream lines, Path lines, Streak lines, Velocity potential, Irrotational and rotational motions. Vortex lines, Equation of Continuity. Lagrangian and Eulerian approach, Euler's equation of motion, Bernoulli's theorem, Kelvin circulation theorem, Vorticity equation, Energy equation for an incompressible flow.

Unit-II

Boundary conditions, Kinetic energy of liquid, Axially symmetric flows, Motion of a sphere through a liquid at rest at infinity, Liquid streaming past a fixed sphere, Equation of motion of a sphere, Sources, Sinks and doublets, Images in a rigid impermeable infinite plane and in impermeable spherical surfaces.

Unit-III

Two-dimensional irrotational motion produced by motion of circular, co-axial and elliptic cylinders in an infinite mass of liquid, Stream functions, Stokes stream functions, Complex velocity potential.

Unit-IV

Conformal mapping, Milne-Thomson Circle theorem, Blasius theorem, Vortex Motion and its elementary properties, Kelvin's proof of permanence, Motion due to rectilinear vortices.

Reference:

- 1. W.H. Besaint and A.S. Ramsey, A Treatise on Hydromechanics, Part II, CBS Publishers, Delhi, 1988.
- 2. F. Chorlton, Textbook of Fluid Dynamics, C.B.S. Publishers, Delhi, 1985.
- 3. S.W. Yuan, Foundations of Fluid Mechanics, Prentice Hall of India Private Limited, New Delhi, 1976.
- 4. M.E.O'Neil and F.Choriton, Ideal and Incompressible Fluid Dynamics, John Wiley & Sons.



M.Sc. (Mathematics) 3rd Semester w.e.f. 2022-2023

MAL- 613: ADVANCED DISCRETE MATHEMATICS (elective)

LT P	Marks for External exam	:80	
5 00(5 credits)	Marks for Internal exam	:20	
	Total	:100	
	Time	: 3hours	

Course outcomes

- Ability to apply mathematical logic to solve problems.
- Understand sets, relations, functions and discrete structures.

• Able to use logical notations to define and reason about fundamental mathematical concepts such as sets relations and functions

Note: The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit –I

Recurrence Relations, Explicit Formula for a Sequence, Solution of Recurrence Relations Homogeneous Recurrence Relations with Constant Coefficients, Particular Solution of a Difference Equation, Recursive Functions, Generating Functions, Convolution of Numeric Functions, Solution of Recurrence Relations by the Method of Generating Function.

Unit – II

The Pigeonhole Principle, Partially Ordered Sets, Hasse Diagram, Logics: Basic Logical Operations, Logical Equivalence Involving Tautologies and Contradictions, Conditional Propositions, Quantifiers, Lattices: Properties of Lattices, Lattices as Algebraic System, Lattice Isomorphism, Bounded, Complemented and Distributive Lattices.

Unit – III

Definitions and Basic Properties of Boolean Algebra, Representation Theorem, Boolean Expressions, Logic Gates and Circuits, Boolean Function, Method to find Truth Table of a Boolean Function, Karanugh map, Expressing Boolean Functions as Boolean Polynomials, Addition of Binary Digits, Half – Adder, Full Adder.

Unit – IV

Graphs: Basic concepts and types of Graphs, Paths and Circuits, Eulerian Circuits, Hamiltonian Circuits, Matrix Representation of Graphs, Planar Graphs, Trees: Definition, and Characterization of Trees Representation of Algebraic Expressions by Binary Trees, Spanning Tree of a Graph, Shortest Path Problem, Minimal Spanning Tree, Tree Searching.

References: 1. Discrete Mathematics by Koleman, Busby & Rose, Pearson's Publication

2. Discrete Mathematical Structures by C.L. Liu, Pearson's Publication

3.Discrete Mathematics by Babu Ram, Pearson's Education, 2011

M.Sc. (Mathematics) 3rd Semester w.e.f. 2022-2023 MAP - 615: MATLAB

- L T P
- 0 0 4 (02 Credits)

Marks for External Exam	: 80
Marks for Internal Exam	: 20
Total	: 100
Time	: 3 Hours

Course outcomes

- Know the basic concepts of MATLAB software.
- Understand the procedures, algorithms, and concepts required in solving specific problems.
- Code solutions to problems in MATLAB, in a legible, debug' able and efficient way.
- Solve different types of mathematical problems and draw various types of graphs using MATLAB.

List of programs using MATLAB

1. As a calculator

- 2. Roots of quadratic equation using command window
- 3. Numerical solutions of equations (single variable)
- 4. Coefficient of friction in each test and find average of it
- 5. Numerical solution of simultaneous linear algebraic equations
- 6. Numerical solution of ordinary differential equation
- 7. Numerical Solution of second order ordinary differential equations
- 8. Create a matrix and find its transpose, inverse and determinant
- 9. To find eigen value and eigen vector of given matrix.
- 10. Create a matrix using zeroes, ones, eye and linespace commands and an another vector, then replace a particular row or column by the 5th root corresponding to that vector.
- 11. Using input and disp command
- 12. Showing vectorized role of fprintf command.
- 13. Plotting a function and its first three derivatives on same plot/ figure.
- 14. Hold on and hold off command
- 15. Plot light intensity vs. distance using label, title, axis text, legand etc. commands.
- 16. Find the sum of the first n terms of the series $\sum_{k=1}^{n} (-1)^{k} K/2^{k}$ using loop. Execute the script file for given n.
- 17. Using nesting loop and conditional statement.
- 18. Write a function file for given function then use it.
- 19. To find subtraction; multiplication & division operation for given two polynomials.
- 20. To find roots & derivatives of given polynomial.
- 21. Program on curve fitting
- 22. Find minimum & maximum value for given function.

Note: Out of the list as above, a student has to perform at least 15 (fifteen) programs in the semester. Five more programs can be done of their own choice.

MAP- 617: SEMINAR

- L T P 2 0 0 (2 Credits)

Marks for Internal Exam : 20 : 20 Total

M.Sc. (Mathematics) 4th Semester w.e.f. 2022-2023 MAL -602: FUNCTIONAL ANALYSIS

- L T P 5 0 0(5 Credits)

Marks for External Exam	: 80
Marks for Internal Exam	: 20
Total	: 100
Time	: 3 Hours

Course outcomes

- Be familiar with the completeness in normed linear spaces. •Understand the concepts of bounded linear transformation, equivalent formulation of continuity and spaces of bounded linear transformations.
- Describe the solvability of linear equations in Banach Spaces, weak and strong convergence and their equivalence in finite dimensional space.
- Learn the properties of compact operators.
- Understand uniform boundedness principle and its consequences.
- **Note:** The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit-I

Normed linear spaces, metric on normed linear spaces, Holder's and Minkowski's inequality, completeness of quotient spaces of normed linear spaces, Completeness of I_p , L^p , R^n , C^n and C[a,b]. Bounded linear transformation, Equivalent formulation of continuity, Spaces of bounded linear transformation, Continuous linear functional, conjugate spaces.

Unit-II

Fundamental Theorems, Hahn Banach extension theorem (Real and Complex form) Riesz representation theorem for bounded linear functional on L^p and C [a,b] and their consequences, Second Conjugate spaces, Reflexive spaces, uniform boundedness principle and its consequence, open mapping theorem and its application, projections, closed graph theorem Equivalent norms.

Unit-III

Compact operators and its relation with continuous operators, compactness of linear transformation on a finite dimensional space, properties of compact operators, compactness of the limit of the sequence of compact operators, Fixed point, Banach Contraction Principle and its application to solve Matrix equation, Differential Equations, Picard's Theorem and Picard-Lindeloff Theorem.

Unit-IV

Inner product spaces, Hilbert spaces Schwarz's inequality, Hilbert space as normed linear space, convex sets in Hilbert spaces. Projection theorem, orthonormal systems and Gram-Schmidt Orthogonalization Process, Bessel's inequality, Parseval's identity, Conjugate of a Hilbert space, Riesz representation theorem for continuous functional on a Hilbert space.

References:

- 1. E. Kreyszig, Introductory Functional Analysis with Applications, John Wiley & Sons, New York, 1978.
- 2. A.E. Taylor, Introductin to Functional Analysis, John Wiley and Sons, New York, 1958.
- 3. K. Yosida, Functional Analysis, 3rd edition Springer Verlag, New York, 1971.
- 4. Walter Rudin, Functional Analysis, Tata McGraw Hill Publishing Company Ltd., New Delhi, 1973.
- 5. A.H.Siddiqi, Khalil Ahmad, P. Manchanda, Intoduction to Functional Anaiysis with Applications, Anamaya Publishers, New Delhi.

M.Sc. (Mathematics) 4th Semester w.e.f. 2022-2023

MAL -604: INTEGRAL EQUATIONS

L T P 5 0 0 (5Credits) Marks for External Exam :80 Marks of Internal Exam :20

Course outcomes

- Understand the methods to reduce Initial value problems associated with linear differential Understand equations to various integral equations.
- Categorise and solve different integral equations using various techniques .
- Describe importance of Green's function method for solving boundary value problems associated with non-homogeneous ordinary and partial differential equations, especially the Sturm-Liouville boundary value problems.
- **Note:** The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit -I

Definitions of Integral Equations and their classification.Relation between integral and differential equations, Fredholm integral equations of second kind with separable kernels.Eigen Values and Eigen functions.Reduction to a system of algebraic equations.An approximate Method.Method of successive approximations.Iterative scheme.Condition of convergence and uniqueness of series solution.Resolvent kernel and its results.Fredholm theorems

Unit-II

Solution of Volterra's integral equations by iterative scheme.Successive approximation.Resolvent kernel. Integral transform methods: Fourier transform, Laplace transform, Convolution integral, Application to Volterra integral equations with Convolution type kernels, Abel's equations.

Unit-III

Symmetric kernel.Complex Hilbert space. Orthonormal system of functions, Fundamental properties of eigen values and eigen functions for symmetric kernels. Expansion in eigen function and bilinear form, Hilbert Schmidt theorem, Solution of integral equations with symmetric kernels Singular Integral Equations - Inversion formula for singular integral equation with kernel of type (h(s) - h(t) - a, 0 < a < 1).

Unit-IV

Dirac Delta Function. Green's function approach to reduce boundary value problems of a self-adjoint differential equation with homogeneous boundary conditions to integral equation forms. Auxiliary problem satisfied by Green's function. Modified Green's function.

Reference:

- 1. R.P. Kanwal, Linear Integral Equation. Theory and Techniques, Academic Press, New York, 1971.
- 2. S.G. Mikhlin, Linear Integral Equations (translated from Russian), Hindustan Book Agency, 1960.
- 3. Abdul J. Jerri, Introduction to Integral Equations with Applications.
- 4. Hildebrand. F.B Method of Applied Mathematics

M.Sc. (Mathematics) 4th Semester w.e.f. 2022-2023 MAL -606: DIFFERENTIAL GEOMETRY

L T P

5 0 0(5 Credits)

Marks for External Exam: 80Marks for Internal Exam: 20Total: 100Time: 3 Hours

Course outcomes

- Can examine the length and parametrization of curves
- The definitions of curvature and torsion and can apply these
- Knows the local canonical form of curves
- knows the contents and the significance of the Jordan curve theorem and the isoperimetric inequality.
- Can examine the properties of surfaces using different expressions for surfaces.

Note: The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit-I

Curves with torsion: Tangent, Principal Normal, Curvature, Binormal, Torsion, SerretFrenet formulae, Locus of centre of spherical Curvature.

Unit-II

Envelopes: Surfaces, Tangent plane, Envelope, Characteristics, Edge of regression.

Unit-III

Curvilinear Co-ordinates: First order magnitude, Directions on a surface, Second order magnitudes, Derivative of unit normal, Principal directions and curvatures.

Unit-IV

Geodesics: Geodesics property, Equations of geodesics, Torsion of a geodesics.

References:

- 1. C.E., Weatherburn, Differential Geometry of Three Dimensions.
- 2. Differential Geometry by Schaums Series

M.Sc. (Mathematics) 4th Semester w.e.f. 2022-2023 MAL 608: ALGEBRAIC CODING THEORY (elective)

L T P

5 0 0(5 Credits)

Marks for External Exam	: 80
Marks for Internal Exam	: 20
Total	: 100
Time	: 3 Hours

Course outcomes

- To learn how codes in mathematics are used for error correction and data transmission.
- To comprehend the algebraic structure of linear codes viewed as a vector space over a finite field
- **Note:** The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit – 1

Block codes. Minimum distance of a code.Decoding principle of maximum likelihood.Binary error detecting and error correcting codes.Group codes. Minimum distance of a group code (m, m+1) parity check. Double and triple repition codes. Matrix codes. Generator and parity check matrices. Dual codes. Polynomial codes. Exponent of a polynomial over the binary field.Binary representation of a number.Hamming codes.Minimum distance of a Hamming code. (Chapter 1,2,3 of the book given at Sr. No.1).

Unit – II

Finite fields.Construction of finite fields.Primitive element of a finite field.Irreducibility of polynomials over finite fields.Irreducible polynomials over finite fields.Primitive polynomials over finite fields.Automorphism group of GF(qn). Normal basis of GF (qn).The number of irreducible polynomials over a finite field.The order of an irreducible polynomial. Generator polynomial of a Bose- Chaudhri- Hocqhenghem codes (BCH codes) construction of BCH codes over finite field. (Chapter 4 of the book given at Sr. No. 1 and Section 7.1 to 7.3 of the book given at Sr. No.2)

Unit – III

Linear codes.Generator matrices of linear codes. Equivalent codes and permutation matrices. Relation between generator and parity-check matrix of linear codes over a finite field.Dual code of a linear code.Self Dual codes.Weight distribution of a linear code.Weight enumerator of a linear code.Hadamard transform. Macwilliams identity for binary linear codes.

Maximum distance separable codes.(MDS codes).Examples for MDS codes. Characterization of MDS codes in terms of generator and parity check matrices. Dual code of a MDS code.Reed Solomon codes.(Chapter 5&9 of the book at Sr. No. 1).

Unit – IV

Hadamard matrices. Existence of a Hadamard codes from Hadamard matrices cyclic codes. Generator polynomial of a cyclic code. Check polynomial of a cyclic code. Equivalent code & dual code of a cyclic code.Idempotent generator of a cyclic code.Hamming and BCH codes as cyclic codes.Perfect codes.The Gilbert-varsha-move and Plotkin bounds.Self dual binary cyclic codes.(Chapter 6&11 of the book given at Sr. No.1).

Refrences:

L.R. Vermani: Elements of Algebraic coding theory (Chapman and Hall Mathematics)
Steven Roman: Coding and information Theory (Springer Verlag)

M.Sc. (Mathematics) 4th Semester w.e.f. 2022-2023

MAL 610: MECHANICS OF SOLIDS-II (elective)

L T P

5 0 0(5 Credits)

Marks for External Exam	: 80
Marks for Internal Exam	: 20
Total	: 100
Time	: 3 Hours

Course outcomes

- Two- dimensional problems: plane stress, airy stress.
- Spring dashpot, Maxwell and kalvin models.
- Torsion and stress functions.
- Solution of eule's equation by Ritz, galerkin and Kantorovich method. s

Note: The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit-I

Two-dimensional Problems: Plane stress. Generalized plane stress. Airy stress function. General solution of Biharmonic equation. Stresses and displacements in terms of complex potentials. The structure of functions of $\phi(z)$ and $\psi(z)$. First and second boundary value problems in plane elasticity, Thick-walled tube under external and internal pressures.

Unit-II

Viscoelasticity: Spring & Dashpot, Maxwell & Kelvin Models, Three parameter solid, Correspondence principle & its application to the Deformation of a viscoelastic Thick-walled tube in Plane strain.

Unit-III

Torsion:Torsion of cylindrical bars. Tortional rigidity.Torsion and stress functions.Lines of shearing stress. Simple problems related to circle, ellipse and equilateral triangle.

Waves: Propagation of waves in an isotropic elastic solid medium. Waves of dilatation and distortion.Plane waves. Elastic surface waves such as Rayleigh and Love waves.

Unit-IV

Variational methods - Theorems of minimum potential energy. Theorems of minimum complementary energy. Reciprocal theorem of Betti and Rayleigh. Deflection of elastic string, central line of a beam and elastic membrane. Solution of Euler's equation by Ritz, Galerkin and Kantorovich methods.

References

- 1. I.S. Sokolnikoff, Mathematical Theory of Elasticity, Tata McGraw Hill Publishing Company Ltd., New Delhi.
- 2. Y.C. Fung, Foundations of Solid Mechanics, Prentice Hall, New Delhi.
- 3. S. Timoshenko and N. Goodier, Theory of Elasticity, McGraw Hill, New York.
- 4. W. Flugge, Viscoelasticity, Springer VerL.

M.Sc. (Mathematics) 4th Semester w.e.f. 2022-2023 MAL-612: ADVANCED FLUID MECHANICS (elective)

L T P

5 0 0(5 Credits)

Marks for External Exam	: 80
Marks for Internal Exam	: 20
Total	: 100
Time	: 3 Hours

Course outcomes

- Apply the fundamentals of kinematics and conservation laws of fluid flow systems.
- Apply the principles of high and low Reynolds number flows to fluid flow systems.
- Review the concepts of boundary layer and flow in transition.
- Analyse and apply the fundamentals of turbulent flow to various fluid flow systems.
- Apply the fundamentals of one dimensional isentropic flow to variable area duct.
- Analyse the principles of normal shock formation and its effects.
- **Note:** The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit-I

Stress components in a real fluid, Relations between rectangular components of stress, Connection between stresses and gradients of velocity. Navier-Stoke's equations of motion. Exact Solution of Navier-Stoke's equations of motion- Couette flows and Generalized Couette flow between two parallel plates, Plane Poiseuille flow, Hagen Poiseuilleflow,Flow through tubes of uniform cross section in form of circle, annulus, ellipse and equilateral triangle under constant pressure gradient. Unsteady flow over a flat plate.

Unit-II

Dynamical similarity: Buckingham π -theorem. Reynolds number, Eckert Number, Froude Number, Application of pi- theorem to viscous and compressible fluid.

Unit-III

Boundry Layer Flow: Prandtl's boundary layer. Boundary layer equations in twodimensions.Blasius solution.Boundary layer thickness.Displacement thickness.Karman integral equations.Separation of boundary layer flows.

Unit-IV

Wave motion in a gas: Speed of Sound, Equation of motion of a gas, Subsonic, Sonic and supersonic flows of a gas, Isentropic gas flows, Flow through a nozzle.



Referencs:

- 1. F. Chorlton, Textbook of Fluid Dynamics, C.B.S. Publishers, Delhi, 1985.
- 2. H. Schlichting, Boundary Layer Theory, McGraw Hill Book Company, New York, 1979.
- 3. A.D. Young, Boundary Layers, AIAA Education Series, Washington DC, 1989.
- 4. S.W. Yuan, Foundations of Fluid Mechanics, Prentice Hall of India Private Limited, New Delhi, 1976

M.Sc. (Mathematics) 4th Semester w.e.f. 2022-2023 MAL 614: PARTIAL DIFFERENTIAL EQUATION (elective)

L T P

5 0 0(5 Credits)

Marks for External Exam	: 80
Marks for Internal Exam	: 20
Total	: 100
Time	: 3 Hours

Course outcomes

- Apply a range of techniques to find solutions of standard Partial Differential Equations (PDE).
- Demonstrate accurate and efficient use of Fourier analysis techniques and their applications in the theory of PDE's.
- Demonstrate capacity to model physical phenomena using PDE's (in particular using the heat and wave equations).
- Apply problem-solving using concepts and techniques from PDE's and Fourier analysis applied to diverse situations in physics, engineering, financial mathematics and in other mathematical contexts.

Note: The examiner is requested to set **nine** questions in all taking two questions from each unit and one **compulsory** question. The compulsory question will consist of four parts and will be distributed over the whole syllabus. The candidate is required to attempt **five** questions selecting one from each unit and the compulsory question.

Unit -I

Solution of Partial Differential Equation. Transport equation-initial value problem, Non homogeneous equation,Laplace equation-fundamental solution, Mean value formulas, Properties of harmonic functions, Green function, Energy methods

Unit -II

Heat equation-fundamental solution, solution of initial value problems, non homogeneous equations, Mean value formula. Wave Equation-solution by spherical means, non homogeneous equations, Energy methods

Unit -III

Nonlinear first order PDE- complete integrals, Envelopes, Characteristics, Hamilton Jacobi equations, Hamilton's ODE, Hopf-Lax formula, Weak solutions, Uniqueness

Unit -IV

Representation of Solutions:Separation of variables, Similarity solutions (Plain & Traveling waves solutions, Similarity under scaling), Fourier & Laplace transform,Hopf-Cole,Hodograph&Legendere transform, Potential functions.

References:

- 1. L.C. Evans, Partial Differential Equations, Graduate studies in mathematics, Volume-19, AMS, 1998.
- 2. I.N. Sneddon, Elements of Partial Differential Equations, McGraw Hill international
- 3. An Introduction to Partial Differential Equation Yehuda Pinchover and Jacob Rubinstein, CAMBRIDGE University press 2005.

M.Sc. (Mathematics) 4th Semester w.e.f. 2022-2023 MAP – 616: LATEX (Lab)

L T P

0 0 4(02 Credits)

Marks for External Exam	: 80
Marks for Internal Exam	: 20
Total	: 100
Time	: 3 Hours

Course outcomes

- Typeset mathematical formulae using LaTeX.
- Use the preamble of LaTeX file to define document class and layout options.
- Use nested list and enumerate environments within a document.
- Use tabular and array environments within LaTeX document.
- Use various methods to either create or import graphics into a LaTeX document.
- Use the beamer package to create presentations.
- Define and use new commands within LaTeX.
- Use Theorem, Corollary, and other environments.
- Use BibTeX to maintain bibliographic information and to generate a bibliography for a particular document.

List of programs using LATEX

- 1. Tabular environment.
- 2. Create horizontal and vertical lines in table using LATEX commands
- 3. Multicolumn command.
- 4. Display role of cline command .
- 5. Math and math display mode.
- 6. Mathematical expression using some mathematical operation symbols .
- 7. Array environment.
- 8. Nesting array and tabular
- 9. Equation array and equation array star.
- 10. Role of nonumber command.
- 11. Nesting of array and tabular.
- 12. Framed equations using fbox command.
- 13. Signum and Dirichlet function.
- 14. Role of itemize environment.
- 15. Enumerate environment nesting of it.
- 16. Section and subsection.

- 17. Letter using LATEX.
- 18. Quote and quotation environments.
- 19. Role of displaystyle.
- 20. Program using mbox command.
- 21. Write some equation using derivative and integral symbols .
- 22. Verse and Descriptive environment.

Note: Out of the list as above, a student has to perform at least 15 (fifteen) programs in the semester. Five more programs can be done of their own choice.

MAP- 618: SEMINAR

L T P 2 0 0 (2 Credits)

Marks for Internal Exam : 20 : 20 Total